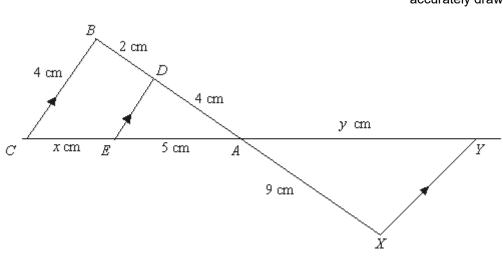
Q1.

Diagram **NOT** accurately drawn



### Edexcel Maths GCSE - Congruency and Similarity (FH)

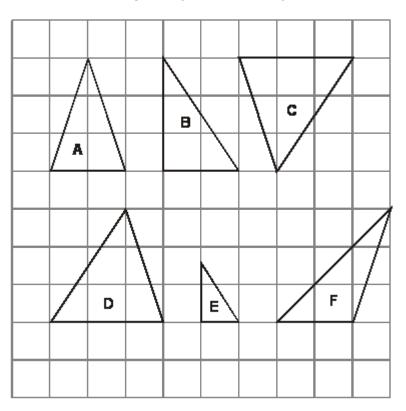
CEAY and BDAX are straight lines. XY, ED and CB are parallel. AE = 5 cm. AX = 9 cm. AD = 4 cm. BC = 4 cm. BD = 2 cm. CE = x cm. XY = y cm.

Find the value of x and the value of y.

*x* = ..... *y* = .....

(Total 4 marks)

**Q2.** These triangles have been drawn on a centimetre grid.



(a) Write down the letters of the **two** triangles that are congruent.

..... and .....

(1)

(b) Write down the letters of **two different** triangles that are similar.

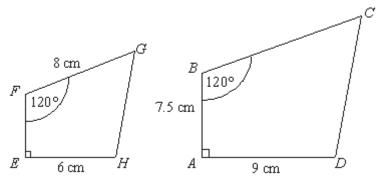
..... and .....

(1)

(c) Find the area of triangle **D**.

.....

(1) (Total 3 marks) **Q3.** Shapes *ABCD* and *EFGH* are mathematically similar.



Diagrams **NOT** accurately drawn

(a) Calculate the length of BC.

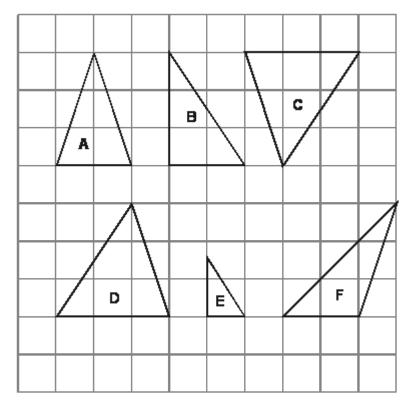
..... cm

(2)

(b) Calculate the length of EF.

..... cm

(2) (Total 4 marks)



**Q4.** These triangles have been drawn on a centimetre grid.

(a) Write down the letters of the **two** triangles that are congruent.

..... and .....

(1)

(b) Write down the letters of **two different** triangles that are similar.

..... and .....

(1)

(c) Find the area of triangle **D**.

.....

(1) (Total 3 marks)

(3)

Q5.

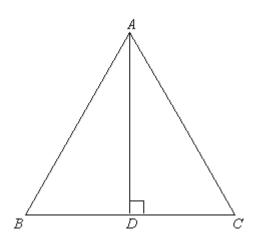


Diagram NOT accurately drawn

ABC is an equilateral triangle. D lies on BC. AD is perpendicular to BC.

(a) Prove that triangle ADC is congruent to triangle ADB.

(b) Hence, prove that 
$$BD = \frac{1}{2}AB$$
.

(2) (Total 5 marks)

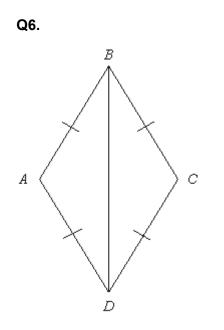
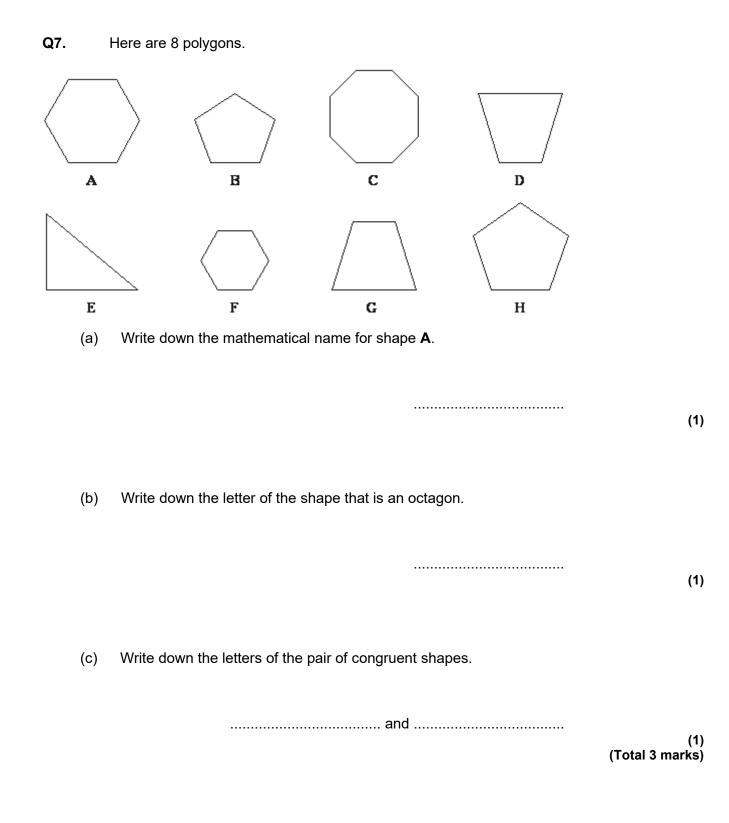


Diagram NOT accurately drawn

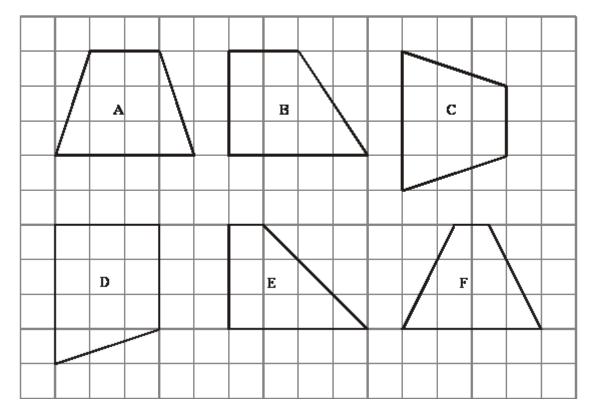
In the diagram, AB = BC = CD = DA.

Prove that triangle *ADB* is congruent to triangle *CDB*.

(Total 3 marks)



### Edexcel Maths GCSE - Congruency and Similarity (FH)



**Q8.** Here are 6 shapes drawn on a grid.

Two of these shapes are congruent.

(a) Write down the letters of these two shapes.

..... and .....

(1)

(b) On the grid below, draw a shape that is congruent to shape **P**.

| Р |      |  |  |  |  |  |  |
|---|------|--|--|--|--|--|--|
|   | <br> |  |  |  |  |  |  |
|   |      |  |  |  |  |  |  |
|   |      |  |  |  |  |  |  |

(1) (Total 2 marks)



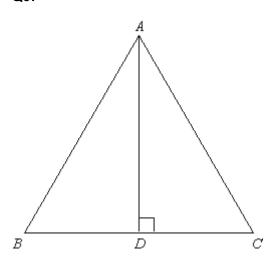


Diagram NOT accurately drawn

ABC is an equilateral triangle. D lies on BC. AD is perpendicular to BC.

Prove that triangle ADC is congruent to triangle ADB.

(Total 3 marks)

## M1.

| Working  | Answer           | Mark | Additional Guidance  |
|--|------------------|------|--|
| $\frac{x}{5} = \frac{2}{4}$                                    | <i>x</i> = 2.05  |      | <b>M1</b> a correct expression for <i>x</i> involving ratios of sides, e.g. $\frac{x}{5} = \frac{2}{4}$ oe |
| $\frac{y}{x+5} = \frac{9}{6}$ or $\frac{y}{9} = \frac{x+5}{6}$ | <i>y</i> = 11.25 |      | <b>A1</b> cao  |

Total for Question: 4 marks

M2.

|     | Working | Answer              | Mark | Additional Guidance         |
|-----|---------|---------------------|------|-----------------------------|
| (a) |         | C and D             | 1    | <b>В1</b> сао               |
| (b) |         | B and E             | 1    | <b>B1</b> cao               |
| (c) |         | 4.5 cm <sup>2</sup> | 1    | B1 cao                      |
|     |         |                     |      | Total for Question: 3 marks |

# M3.

|     | Working                     | Answer | Mark | Additional Guidance  |  |  |  |
|-----|-----------------------------|--------|------|--|--|--|--|
| (a) | $\frac{3}{2} \times 8$      | 12     |      | 9 6 8 6<br>M1 for <sup>6</sup> or <sup>9</sup> or <sup>6</sup> or <sup>8</sup><br>A1 cao   |  |  |  |
| (b) | 2<br>3 × 7.5                | 5      |      | <b>M1</b> for $\frac{9}{6}$ or $\frac{9}{9}$ or $\frac{7.5}{7.5}$ or $\frac{7.5}{9}$ or $\frac{12"}{8}$ or $\frac{8}{12"}$<br>or $\frac{12"}{7.5}$ or $\frac{7.5}{12"}$<br><b>A1</b> cao |  |  |  |
|     | Total for Question: 4 marks |        |      |  |  |  |  |

### M4.

|     | Working | Answer              | Mark | Additional Guidance         |
|-----|---------|---------------------|------|-----------------------------|
| (a) |         | C and D             | 1    | B1 cao                      |
| (b) |         | B and E             | 1    | <b>В1</b> сао               |
| (c) |         | 4.5 cm <sup>2</sup> | 1    | B1 cao                      |
|     |         |                     |      | Total for Question: 3 marks |

## M5.

|     | Working  | Answer | Mark | Additional Guidance   |
|-----|--|--------|------|---|
| (a) | $AB = AC \text{ (equilateral triangle)}$ $AD \text{ is common}$ $ADC = ADB (= 90^{\circ} \text{ given})$ $\Delta ADC \equiv \Delta ADB \text{ (RHS)}$ $OR$ $DAC = DAB \text{ (since } ACD = ABD \text{ and}$ $ADC = ADB$ $AB = AC \text{ (equilateral triangle)}$ $AD \text{ is common}$ $\Delta ADC \equiv \Delta ADB \text{ (SAS)}$ $OR$ | Proof  |      | <ul> <li>M1 for any three correct statements (which do not have to be justified) that together lead to a congruence proof (ignore irrelevant statements)</li> <li>A1 for a full justification of these statements</li> <li>A1 for RHS, SAS, AAS, ASA or SSS as appropriate</li> <li>NB The two A marks are independent</li> </ul> |
|     | DAC = DAB (since ACD = ABD and<br>ADC = ADB)<br>AD is common<br>ACD = ABD (equilateral triangle)   |        |      |   |

# Edexcel Maths GCSE - Congruency and Similarity (FH)

| $\triangle ADC \equiv \triangle ADB$ (AAS)  |       |  |
|---|-------|--|
| BD = DC (congruent Δs)<br>BC = AB (equilateral Δs)<br>Hence BD = $\frac{1}{2}$ AB | Proof | <b>B1</b> for <i>BD</i> = <i>DC</i> and <i>BC</i> = <i>AB</i><br><b>B1</b> for justification of these<br>statements and completion of<br>proof |
|   |       | Total for Question: 5 marks  |

### M6.

| Working   | Mark | Additional Guidance   |  |  |  |
|---|------|---|--|--|--|
| AD = CD equal sides<br>AB = CB equal sides<br>BD is common<br>ADB is congruent to $CDB$ (SSS) |      | <b>B2</b> for two of $AD = CD$ , $AB = CB$ , $BD$ is common<br><b>OR</b> for $BD$ common and all other sides equal in<br>length (it must be clear that the 'other sides' relate<br>to the two triangles)<br>( <b>B1</b> for one of these. Note: All sides are of the<br>same length alone is ambiguous and gains <b>B0</b> )<br><b>B1</b> for proof of congruence (SSS or SAS or ASA)<br>dependent upon THREE identities (with reasons) |  |  |  |
| Total for Question: 3 mark  |      |   |  |  |  |

# M7.

|     | Working | Answer             | Mark | Additional Guidance        |
|-----|---------|--------------------|------|----------------------------|
| (a) |         | Regular<br>hexagon | 1    | <b>B1</b> (accept hexagon) |
| (b) |         | D                  | 1    | B1 cao                     |

| (c) | D and G | 1 | <b>B1</b> for both, in any order |
|-----|---------|---|----------------------------------|
|     |         |   | Total for Question: 3 marks      |

## M8.

|     | Answer                      | Mark | Additional Guidance  |  |  |  |
|-----|-----------------------------|------|--|--|--|--|
| (a) | A and C                     | 1    | <b>B1</b> c for A and C or C and A                                   |  |  |  |
| (b) | Shape drawn                 |      | <b>B1</b> for correct shape, any orientation or reflection,<br>±2 mm |  |  |  |
|     | Total for Question: 2 marks |      |  |  |  |  |

### M9.

| Working   | Answer | Mark | Additional Guidance   |
|---|--------|------|---|
| AB = AC (equilateral triangle)<br>AD is common<br>ADC=ADB (= 90° given)<br>ΔADC ≡ ΔADB (RHS)  | Proof  |      | M1 for any three correct statements<br>(which do not have to be justified) that<br>together lead to a congruence proof<br>(ignore irrelevant statements)<br>A1 for a full justification of these statements |
| OR  |        |      | A1 for RHS, SAS, AAS, ASA or SSS as appropriate   |
| DAC = DAB (since $ACD =ABD$ and $ADC = ADB$ )<br>AB = AC (equilateral triangle)<br>AD is common<br>$\triangle ADC \equiv \triangle ADB$ (SAS) |        |      | NB The two A marks are independent  |

| OR   |  |  |
|--|--|--|
| DAC = DAB (since $ACD =ABD$ and $ADC = ADB$ )<br>AD is common<br>ACD = ABD (equilateral<br>triangle)<br>$\triangle ADC \equiv \triangle ADB$ (AAS) |  |  |

**Total for Question: 3 marks** 

**E3.** Those candidates who worked with scale factors were usually successful. Errors were more common in part (b) where some candidates multiplied 7.5 by the scale factor rather than divide. A quick look at the diagram ought to have alerted these candidates to the fact that the length of *EF* could not possibly be 11.25 cm. Many candidates, though, did not work with scale factors but assumed that because *AD* was 3 cm longer than *EH* then each side in *ABCD* was 3cm longer than the corresponding side in *EFGH*. This resulted in 11 cm and 4.5 cm being very common incorrect answers in part (a) and part (b) respectively.

**E5.** Part (a) was very poorly answered. It was good to see some responses in which statements and justifications were laid out correctly but the majority of candidates had little idea of how to set out a formal proof of congruency. Statements were often vague and general, e.g. 'all sides are the same'. Even when candidates were able to give three correct statements it was not uncommon for the incorrect reason for congruency to be given – most frequently SAS when it should have been RHS. Full justification was rare. BD = DC was stated in numerous responses with candidates failing to realise that this was a consequence of congruency. The most common errors were not justifying the statements made and not providing the reason for congruency. Some candidates thought that AAA and ASS were sufficient for congruency. Very often the working was difficult to follow. More candidates were able to gain one mark in part (b) but very few realised they needed to use congruency to justify BD = DC.

**E6.** Candidates understanding of congruency was very good, however it is clear that formal congruency proofs have not been covered by very many centres. Very few candidates were able to quote the requirements for two triangles to be congruent and therefore acceptable proofs were rare. The pairing of corresponding sides was weak and many attempts would just quote vague facts such as 'all the sides are equal'. Some candidates tried to use equal angles but rarely were any reasons ever given for their two angles being equal in size.

Many candidates assumed that the symbols on each of the sides implied parallel lines.

**E8.** Writing down the correct letters of the two shapes that were congruent resulted in a 79% success rate for part (a). Use of tracing paper would have ensured accuracy.

In part (b) there appeared to be a fairly good understanding of the word 'congruent' with just over half the candidates drawing a shape that was identical to the given one. It would have been sufficient to merely draw the shape again a few squares to the right to earn full marks. However, for some reason, possibly because they did not understand what was required, many inverted the shape, rotated the shape or reflected the shape which resulted in the task being made much more demanding.

**E9.** This proved to be difficult for most candidates. Few had a clear idea of what a congruence proof entails and were content to appeal to symmetry. Better candidates were able to marshal some ideas although many made the assumption (they are not told it in the question) that the perpendicular to the base of an equilateral triangle bisects the base. This fact would of course be a consequence of the proof and as such cannot be part of the proof. Other candidates assumed that proving that the triangles were equiangular would do, or quoted SAS when A was not the included angle.